# SUMMER MATH PACKET FOR STUDENTS RISING TO PRECALCULUS

# Provided by Cox Math Tutoring

Directions: Complete the following problems without the use of a calculator, unless the problem is accompanied by

a calculator icon:



#### 1. Evaluate each of the following expressions.

1.1. 
$$\frac{3}{16} + \frac{1}{8}$$

1.2. 
$$\frac{5}{8} - \frac{5}{12} + \frac{1}{6}$$

$$1.3. \qquad \frac{4}{5} \cdot \frac{1}{2} \cdot \frac{3}{4}$$

1.4. 
$$\frac{27-35}{4}$$

1.5. 
$$\frac{\frac{\frac{1}{5}(-8-9)}{\frac{-1}{3}}}$$

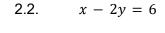
1.6. 
$$5^{-1} + 2^{-3}$$

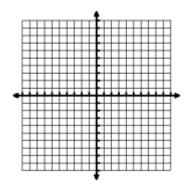
1.7. 
$$\left(\frac{3}{2}\right)^{-2} - 2^2$$

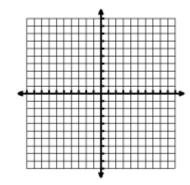
1.8. 
$$-3 + \frac{3}{7}$$

# 2. Graph each equation.

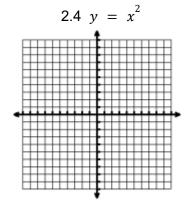
2.1. 
$$y = -3x + 2$$







$$2.3 \quad y = \sqrt{x}$$



3. Describe the transformations in the graphs from the parent function  $f(x) = x^2$ 

3.1. 
$$g(x) = -(x+4)^2 - 3$$

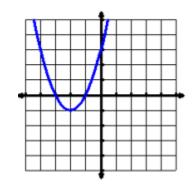
3.2. 
$$h(x) = 2(x-1)^2 + 6$$

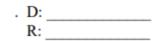
3.3. 
$$m(x) = 3 - (x + 2)^2$$

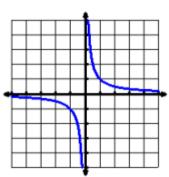
4. Give the domain and range of the following in interval notation.

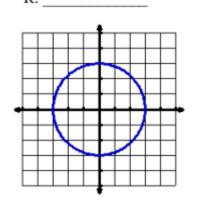


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### 5. Factor completely.

5.1. 
$$x^3 - 7x^2 + 6x$$

4.3

5.2. 
$$3x^2 - 75$$

4.4

$$5.3. - 8x^3 + 40xy + 112y^2$$

5.4. 
$$x^3 - 27$$

5.5. 
$$16x^2 - 24x + 9$$

# 6. Solve by factoring.

6.1. 
$$x^2 - 49 = 0$$

6.2. 
$$6x^2 - 10x = 4$$

6.3. 
$$5x^2 - 37x + 14 = 0$$

$$6.4. 90x^4 - 10x^2 = 0$$

7. Solve by either the quadratic formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  or completing the square.

7.1. 
$$3x^2 + x - 1 = 0$$

$$7.2. 5x^2 + 8x = -12$$

8. Use the properties of exponents to simplify the following expressions.

8.1. 
$$(2y)(4xy^{-3})$$

8.2. 
$$\frac{18a^2bc^3}{36ab^3c}$$

8.3. 
$$\left(\frac{3}{5}c^2f\right)\left(\frac{4}{3}cd\right)^2$$

8.4. 
$$\frac{(2xy^{-1}z^2)^2}{(3x^{-2}y^5z^{-3})^2}$$

9. Write the following in simplest radical form (your answer should not contain decimals).

9.1. 
$$-\sqrt{175}$$

9.2. 
$$\frac{\sqrt{8x^2}}{\sqrt{2x}}$$

9.3. 
$$\sqrt{27} + \sqrt{108}$$

9.4. 
$$(\sqrt{8} + \sqrt{12})^2$$

9.5. 
$$\sqrt[3]{x^2y^4} \cdot \sqrt[3]{x^5}$$

9.6. 
$$\frac{1}{3+\sqrt{5}}$$

10. Write the following complex numbers in simplest form.

10.1. 
$$\sqrt{-64x^{12}}$$

10.4. 
$$(7-4i)-(-3+6i)$$

10.5. 
$$(3 + 4i)(5 - 2i)$$

10.3. 
$$\frac{4-3i}{1+2i}$$

11. Find the reference angle for each of the following angles.

11.4. 
$$-\frac{11\pi}{4}$$

11.3. 
$$\frac{3\pi}{5}$$

12. A point on a terminal side of an angle  $\theta$  in standard position is given. Find the exact value of each of the trigonometric functions of  $\theta$ .

### 13. Name the quadrant in which the angle lies.

13.1. 
$$sin\theta > 0$$
,  $cos\theta < 0$ 

13.2. 
$$cos\theta > 0$$
,  $cot\theta < 0$ 

### 14. Find the exact value of the remaining five trigonometric functions of $\theta$ .

14.1. 
$$sin\theta = \frac{-5}{13}$$
,  $\theta$  in quadrant III 14.2.  $cos\theta = \frac{-1}{4}$ ,  $tan\theta > 0$ 

14.2. 
$$cos\theta = \frac{-1}{4}, tan\theta > 0$$

# 15. Sketch the graph of the following functions.

15.1. 
$$y = 4\cos(x)$$

15.2. 
$$y = sin(3x)$$

16. Sketch a right triangle and solve each of the followin	solve each of the following.
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16.1. The hypotenuse of a right triangle is 5 inches.

If one leg is 2 inches, find the degree measure of each angle.

16.2. At 10 A.M. a building 300 ft. high cast a shadow 50 ft. long. What was the elevation of the sun.